

B. Tech.
(SEM IV) THEORY EXAMINATION 2017-18
THEORY OF AUTOMATA & FORMAL LANGUAGES

Time: 3 Hours

Total Marks: 100

Note: 1. Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

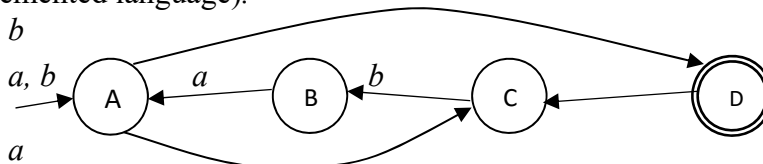
1. Attempt all questions in brief. 2 x 10 = 20

- a. Explain the applications and limitations of finite automata.
- b. Explain what modifications will be required to transform a Finite Automata model into Turing machine.
- c. What is MyHillNerode theorem? Explain.
- d. What is extended transition function δ^* ? Explain with example.
- e. Give the difference between Mealy and Moore machine.
- f. Define and give the difference between positive closure and Kleene closure.
- g. What in nondeterministic PDA? Explain with the help of transition function.
- h. Give the regular expression for set of all strings over $\{0,1\}$ containing exactly three 0's.
- i. Prove or disprove that union and concatenation of two context free languages is also context free.
- j. Explain recursively enumerable languages with example.

SECTION B

2. Attempt any three of the following: 10 x 3 = 30

- a. Explain the purpose of following FA:
 $\delta(q_1, a) = q_1, q_2, \quad \delta(q_1, b) = q_3, \quad \delta(q_2, a) = q_3, q_2$
 q_1 is initial state and $F = \{q_2, q_3\}$
- b. Let the language of FA given below be L . Determine the FA accepting L (i.e. Complemented language).



- c. Prove that for all sets (i) $(S^+)^+ = S^+$, (ii) $(S^+)^* = S^*$
- d. Prove that the language $L = \{a^n b^n c^n | n \geq 0\}$ is neither regular nor context free.
- e. Explain Church's Thesis and prove that Halting problem of Turing machine is undecidable.

SECTION C

3. Attempt any *one* part of the following: 10 x 1 = 10
- (a) Give finite automata for:
i) $L = \{a^n b^{2m} c^{3l} \mid n, m, l \geq 0\}$.
ii) $L = \{a^n b^{2m} \mid 0 < n < 3, m \geq 0\}$.
- (b) Design DFA to accept all string over $\{0, 1\}$ not ending with 10.
4. Attempt any *one* part of the following: 10 x 1 = 10
- (a) Determine the language generated by grammar
 $S \rightarrow Sab \mid aSb \mid abS \mid baS \mid bSa \mid Sba \mid aS \mid a$
- (b) What is inherent ambiguity? Explain with the help of suitable example.
5. Attempt any *one* part of the following: 10 x 1 = 10
- (a) Determine the grammar for language $L = \{a^n b^m \mid n \geq m\}$. Also explain the type of this language.
- (b) Construct context free grammar G corresponding to following context free language, then construct PDA corresponding to G
 $L = \{0^n 1^{2n} \mid n \geq 1\}$
6. Attempt any *one* part of the following: 10 x 1 = 10
- (a) Design PDA for language:
 $L = \{s \in (0, 1)^* \mid \text{number of 0's and 1's are not equal in every string of } s\}$.
- (b) Construct a Turing machine to accept the language $L = \{a^n b^n c^m \mid m, n \geq 0\}$.
7. Attempt any *one* part of the following: 10 x 1 = 10
- (a) Explain variations in Turing machine to make it more capable. How Universal Turing machine can be considered as model of digital computer?
- (b) Explain Modified Post Corresponding Problem. Does the following Post Corresponding Problem have a solution?
 $A = (101, 100, 10, 0, 010), B = (10, 01, 0, 100, 1)$